

Properties of air:



Volume  $V$

# of molecules  $n$

Pressure  $P$

Temperature  $T$

If I increase the volume, pressure decreases at constant temperature.

$V, n$  constant,  $T \uparrow, P \uparrow$

$P, n$  constant,  $T \uparrow, V \uparrow$

Ideal Gas Law:  $PV \propto T$   $PV = nkT$

Consider constant temp:

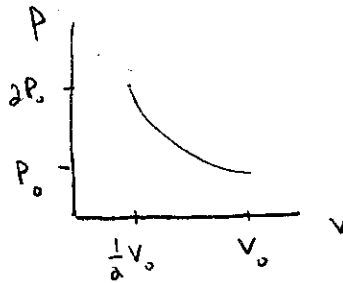


compress volume  $\rightarrow$  pressure increases

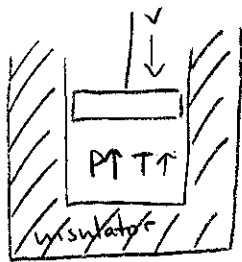
$P \propto \frac{1}{V}$

$PV = \text{const.}$  "isotherm"

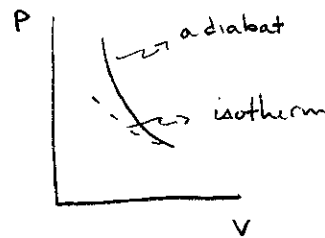
emit heat



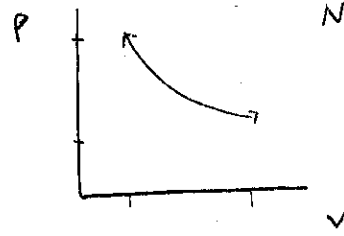
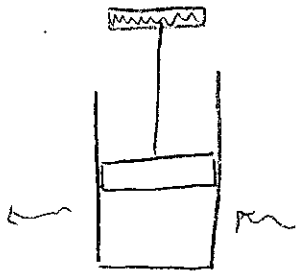
Consider adiabatic: no heat in or out



$PV^\gamma = \text{constant}$



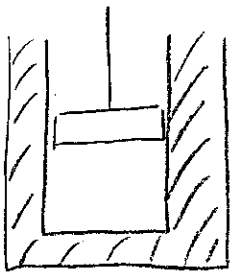
Silly Engine #1: isothermal



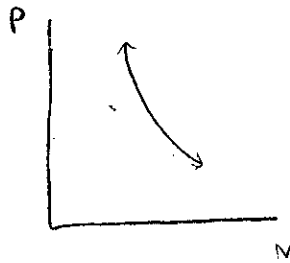
$$\text{Net Work} = \int P dV = 0$$

(No temp gradient - how could there be?)  
isotherm

Silly Engine #2:



adiabatic



No heat flow

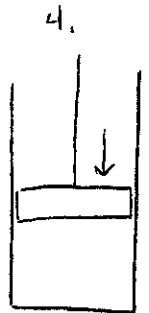
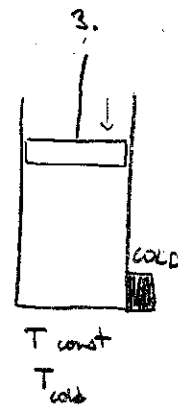
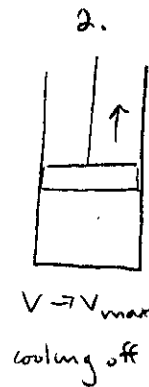
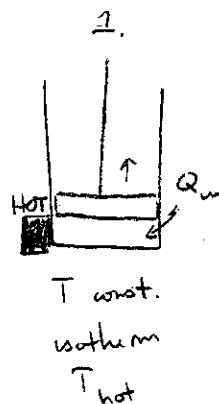
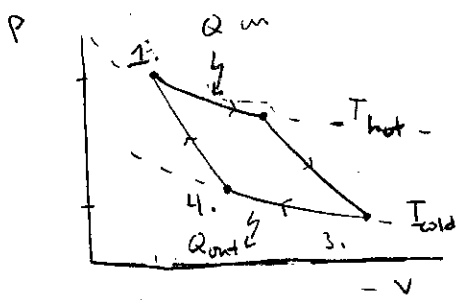
$$\Rightarrow \text{Net Work} = \int P dV = 0$$

To get net work, I need:

- temp diff.
- heat flow
- (• area on PV diagram)

Carnot's Insight: add heat when system is hottest → most efficient engine  
remove heat when system is coldest  
at all other times, no heat flow

perfect Carnot engine



Something important -

Entropy - measure of disorder

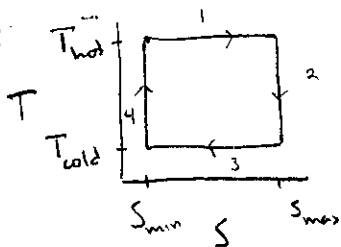
(s) - every process increases disorder  $\Rightarrow$  entropy always increases

$$dS = \frac{dQ}{T}$$

$$\int T \cdot dS = \int P \cdot dV = W$$

$\hookrightarrow$  easier way to find work is to use entropy!

Carnot Cycle:  $(dS=0$  for adiabatic processes!)



$$W = \int T \cdot dS = (T_{hot} - T_{cold}) (S_{max} - S_{min})$$

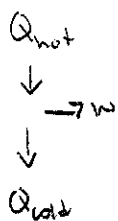
consider step 1:  $\Delta S = \frac{\Delta Q}{T} = \frac{Q_{in}}{T_{hot}}$

$$W = \frac{(T_{hot} - T_{cold}) \times Q_{in}}{T_{hot}}$$

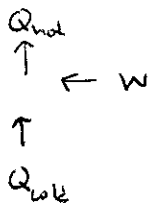
$$\text{efficiency} = \boxed{\epsilon} = \frac{W}{Q_{in}} = \frac{T_{hot} - T_{cold}}{T_{hot}} = \boxed{1 - \frac{T_{cold}}{T_{hot}}} \quad * T \text{ is measured in K}$$

Something else important: Reversibility

engine "reversible" if no unnecessary losses



reverse:



\* a refrigerator is a heat cycle in reverse

\* heat pump: make my house warmer by making outside colder