Mathematical Methods in Python
A companion to
Principles of Planetary Climate

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Preface

This document goes over some basic computer skills that will be useful in doing the problems in the Workbook sections of *Principles of Planetary Climate*, and in reproducing the calculations discussed in the text. It also serves as a quick-start introduction to the Python language, emphasizing those aspects of most interest to applications in the physical sciences.
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Chapter 1

Some basic computer skills
1.1 Basic Skills

To do the labs and the problem sets, you will need some basic computer skills. I will outline these briefly here. The instructions below assume that the exercises will be done using what I’ll call the default setup. In the default setup, the course software and the necessary datasets reside on a centralized server; the student logs on to the server from a workstation that supports the ssh protocol and the X windowing system. The X window system is needed to allow a remote server to write graphics (e.g. a plot, or a graphical user interface) to the screen of the local workstation. The specific instructions below apply most closely to Unix workstations. The necessary skills for using the default setup are:

- Logging in to a Linux server from a workstation on the network.
- Setting things up for the Linux machine to display its graphics on the workstation you are sitting at, using the X windowing system.
- Working with Linux directories and files (commands \texttt{cd,ls,mv,rm,mkdir}).
- Starting up the Python interpreter and using the Python Integrated Development Environment, \texttt{idle}.

1.1.1 Using xterms and logging in to the server

The software that you will be using, as well as the data you will be looking at, resides on a server running the Unix operating system. In the examples, we will suppose that the server is \texttt{climate.myUniversity.edu}; your own server will have a different name, which will be provided by your instructor. To use the software, you will need to log into \texttt{climate}, which you can do from any machine anywhere in the world, as long as the machine has an ssh program. The first step is to get an X terminal window (“xterm” for short) on the screen of the workstation at which you are sitting. If your workstation is a Unix computer the standard window you get when you request a “shell” or a “terminal” window is already an xterm, assuming the system has been started up into a graphical user environment, as is generally the case these days. To get a new xterm, you just need to click on the appropriate icon on the desktop. The specific icon varies somewhat from system to system, but will generally look like a scallop shell or a computer screen.

Macs running OSX are actually running a form of Unix, but the default graphical interface does not use the X windowing system. This will be less confusing if you recall that the ”X” in ”OSX” is actually pronounced ”10”. The standard terminal, or shell, window you get with the OSX terminal tool is not an xterm. While you can issue Unix commands and log onto remote systems for text-based applications by issuing the ssh command in this window, the OSX terminal window does not handle graphics. Further, OSX does not come with the X windowing system installed by default. Fortunately, Appole provides an excellent implementation for X on OSX, which can be installed from the system install disk. If you have your own OSX Mac, or have administrative privileges for some OSX Mac you can use, you can install X11 yourself very easily. All Macs set up for this course should, in principle, already have X11 installed. To get an xterm, you just click on the X11 icon in the toolbar and wait for X to start up. The default windows X puts up on the screen are all xterms. You can make a window go away by typing \texttt{ctrl-d} in the window (meaning hold down the \texttt{ctrl} key and type \texttt{d}. If you want a new xterm, just type \texttt{xtermk} in any existing xterm window, or choose \texttt{terminal} from the \texttt{Applications} menu, and a new one.
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will pop up. Your instructor can show you how to move and resize windows or turn them into icons.

Once you have an xterm on your screen, click the mouse in its window to activate it. You are now ready to log in to the course server. If you happen to be on a Unix workstation with the course data and software installed locally, you can just skip the login step. This is one of the beauties of X and Unix – the system doesn’t really care which computer is actually doing the calculation. This remark applies equally to OSX Macs, provided that Unix versions of the course software have been properly installed.

Now let’s assume that you need to log on to the course server. You’ll need an account to go further: a userid and a password. If you already have an account on climate, you can use that. If not, you can get one of the pre-assigned accounts from the TA. Once you have this data, you can log in. To log in, just issue the command ssh -X -l<USERID> climate.myUniversity.edu from an xterm, where <USERID> is the userid for the course account. Then give your password at the prompt. The -X option tells the server to forward graphical commands to the local X windowing system for handling. On many Linux systems, this option is turned on by default, but it never hurts to include it explicitly. For the more recent versions of Linux, you use ssh -Y instead of -X, so try that if things don’t work with -X.

1.1.2 About the Python Shell and idle

Python is an interpreted language, which means you just type in plain text to an interpreter, and things happen. There is no compilation step, as in languages such as c or FORTRAN. To start up the Python interpreter, just type python from the command line on climate. You’ll get a prompt, and can start typing in python commands. Try typing in 2.5*3+5. and see what happens. To exit the Python interpreter, type ctrl-d.

Eventually, you’ll probably want to put your Python programs, or at least your function definitions, in a file you create and edit with a text editor, and then load it into Python later. This saves you having to re-type everything every time you run. The standard Unix implementation of Python provides an integrated development environment called idle, which bundles a Python interpreter window with a Python-aware text editor. To start up idle on a machine you are sharing with other idle users, log in to the server from an xterm and type idle -n. (The -n option keeps idle from running a separate copy of Python for executing the stuff you run in its interpreter window. For technical reasons it is necessary to do this if more than one user is using idle at a time. Except when debugging very complicated code, you probably won’t notice the difference that the -n option makes) You will get a Python shell window, which is an ordinary Python interpreter except that it allows some limited editing capabilities. The real power of idle comes from the use of the integrated editor. To get an editor window for a new file, just choose New Window from the File menu on the Python Shell window. If you want to work with an existing file instead, just choose Open from the File menu, and pick the file you want from the resulting dialog box. You can type text into the editor window, and cut and paste in a fashion that will probably be familiar to most computer users. You can have as many editor windows open as you want, and cut and paste between them. When you are done with your changes, select Save or Save as from the File menu of the editor window, and respond to the resulting dialog box as necessary. Once you have saved a file, you can run it by selecting Run module from the Run menu.

You can actually use the integrated editor to edit just about any text file, but it has features that make it especially useful for Python files. For example, it colorizes Python key words, automatically indents in a sensible way, and provides popup advice windows that help you remember
how various Python functions are used. As an exercise at this point, you should try creating and saving a short note (e.g. a letter of gratitude to your TA), and then try opening it up again in a new editor window. To exit from idle just choose Exit from the File menu of any window.

Another nice feature of idle is that it will open and allow you to examine any module that Python can import, without your needing to know where it is located. You do this using the Open module item in the File menu. Just type the name of the module you want to look at into the dialog box and it will open into an editor window.

An especially useful feature of the idle editor is that it allows you to execute the Python script you are working on without leaving the window. To do this, just choose Run Script from the Edit menu of the editor window. Then the script will run in the Python shell window. When the script is done running, you can type additional Python commands into the shell window, to check the values of various quantities and so forth.

idle has various other powerful features, including debugging support. You can manage without these, but you should feel free to learn about and experiment with them as you go along.

Once you have written a working Python script and saved it, say, as MyScript.py, you can run it from the command line by typing python MyScript.py. There is no need to start up idle just to run a script.

1.1.3 Running Python Locally

Note that many of the Python-based exercises given in the problem sets do not need the data stored on climate, or the special Python extension modules written for this course. If you have a computer of your own, you can download your own copy of Python from the web site python.org. Implementations are available for Macs, Linux and Windows PC’s. The MacPython implementation, available for both OS9 and OSX Macs provides an excellent integrated development environment that in some ways is superior to idle. You can use your own stand-alone machine for any of the exercises that need only straight Python programming using the standard modules. You can also use your own machine for any exercises involving reading and writing of text data files, if you first download any needed data from climate to your own machine. Also, any Python extension modules that are written as ordinary human-readable Python scripts (e.g. phys.py ) can be just downloaded and put in your python directory, regardless of what kind of machine you are using. However, compiled extension modules, with names like veclib.so need to be compatible with your specific hardware and Python implementation.

In the rest of this tutorial, when we say "Start up the Python interpreter," the choice is up to you whether you use the simple command line interpreter or idle, or perhaps some other integrated Python development environment you might have (e.g. MacPython). For results that produce graphics, and for the use of idle, you must be connected to Python in a way that can display graphics on your screen (e.g. via an xterm). You won’t be reminded of this explicitly in the text. Exercises that don’t produce graphics can be done over any kind of link. "Write and run" a script could mean that you enter it using your favorite editor and run it from the command line, or it could mean using idle. On the usual Mac installation, you can actually start up idle by double-clicking on its icon in the Python folder in your Applications folder, but it turns out this makes it hard for Python to find add-on modules that are stored in non-standard places. For this and a few other technical reasons having to do with display of graphics, I recommend starting idle by opening a terminal window and typing the idle command into the command line, even when running locally.
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In general, I have tried to avoid referring to implementation-dependent details in the rest of this tutorial.
Chapter 2

Introduction to Python
CHAPTER 2. INTRODUCTION TO PYTHON

2.1 Fun with Python

This is a very simple lab designed to help you get used to programming with Python. Throughout this and the rest of the Python labs, it is expected that you will try out all the examples in the Python interpreter window, and make up additional examples on your own until you feel you understand the concept being introduced. For the most part, you won’t be bothered with any further reminders of this expectation.

First, start up the Python interpreter. For this lab, you can type your input directly into the interpreter, if you wish. As you begin to do more complex programs, however, you will want to write your programs using a text editor, and then save them before running. This way, you won’t have to retype everything when you need to correct a mistake in just one or two lines, and you can re-run the program or a modification of it very easily. Although none of the exercises in this lab are complex enough to really require the text editor, you can use this lab as an opportunity to become familiar with the use of the idle editor.

2.1.1 Basic operations

Once you’re at the Python interpreter prompt, try some simple statements using Python like a calculator, e.g.:

\[
\begin{align*}
52.5 & \times 51.2 + 37. \\
\text{a} & = 7. \\
\text{b} & = 10. \\
\text{a} / \text{b} & \\
\text{a} \times \text{b} & \\
\text{a} & = 7 \\
\text{b} & = 10 \\
\text{a} \times \text{b} & \\
\text{a} / \text{b} & \\
2 & \times 1000 \\
1717 & \mod 3
\end{align*}
\]

and so forth. This is so nice, you’ll probably want to load Python onto your laptop and use it in place of a pocket calculator, especially once you learn how to import the standard math functions into your Python world. These examples illustrate the use of floating point numbers, multiplication and addition ("*", "+" and "/") assignment to variables, integers, and exponentiation "**". The final example illustrates the use of the "mod" operator, \(\%\) which is a binary operator applied to integers. The expression \(n \mod m\) yields an integer whose absolute value is less than \(m\), which is the result of subtracting off the maximum possible multiples of \(m\) (if you are familiar with clock arithmetic, this is the operation that turns regular arithmetic into clock arithmetic modulo \(m\)). The assignments to the variables \(a\) and \(b\) illustrate that Python is not a typed language. You do not have to declare the variables as being of a certain type before you use them. They are just names, which are used as long as necessary to refer to some value. This extends not just to numbers, but to all the objects which Python can deal with, including arrays, lists, functions, strings and many other entities which will be introduced shortly. In the example above, first \(a\) and \(b\) are floats, and behave like floats on division. Then they are integers, and behave like integers. The last line illustrates the exponentiation operator, denoted by "**". The large number you get as a result has an "L" tacked on the end, signifying that the result is a long integer, which can have
arbitrarily many digits (until you run out of memory). Python automatically creates this type of integer whenever necessary. The standard Python floating point number has double precision, though Python extensions are available which allow you to specify arbitrary precision for floats as well.

Python also has floating point complex numbers as a native data type. A complex number with real and imaginary parts $a$ and $b$ respectively is written as $a + bj$. All the usual operations apply. After setting $z = 7.5 + 4.47177$ try $z + 1$, $z * z$, $1/z$, $z ** 1.5$ and $z * * z$. If you need to make a complex number out of two real variables, say $x$ and $y$, the easiest way is to use the `complex` function, e.g. $z = \text{complex}(x,y)$. Python does not have complex integers (known as _gaussian integers_ to mathematicians) as a native data type, but you will learn how to define these, and virtually any other specialized type you need, in Section 2.5.1

### 2.1.2 Lists, tuples and strings

Tuples and lists are among the most basic and versatile data structures in Python. Lists contain any kind of data at all, and the elements can be of different types (floats, int, strings, even other tuples or lists). Many functions return tuples or lists. Try out the following examples in the interpreter.

Here's an example showing two ways defining a list and getting at an element:

```python
a = [1,'two']
a[0]
a[1]
b = []
b.append(1)
b.append('two')
b[0]
b[1]
```

In the second part of the example, note that a list, like everything else in Python, is in fact an "object" with actions (called "methods") which you can perform by appending the method name to the object name. The mod operator is useful for making circular lists, which begin over from the first element when one reaches the end. For example, if $a$ is any list, $a[i % \text{len(a)}]$ will access the list as if it were bent around in a circle. The same trick works for any integer-indexed object.

Python distinguishes between lists and tuples. These are similar, except that lists can be modified but tuples cannot. Lists are denoted by square brackets, whereas tuples are denoted by parentheses. The above example is a list rather than a tuple. You can define a tuple, but once defined you cannot modify it in any way, either by appending to it or changing one of its elements. There are a very few cases where Python commands specifically require a tuple rather than a list, in which case you can turn a list (say, `mylist`) to a tuple by using the function `tuple(mylist)`.

Strings are also objects, with their own set of useful methods. For example:

```python
a = 'Five gallons of worms in a 3 gallon barrel!'
a.split()
b = a.split()
print b[0],b[3],b[4]
```
Note that the `split()` method returns a list, whose elements are strings. By the way, in Python, you can use either single quotes or double quotes to enclose a string, as long as you use them consistently within any one string. There is no difference in the behavior of single quoted and double quoted strings. For strings, the `+` operator is concatenation, i.e. `a+b` is the concatenation of the two strings `a` and `b`.

It is very often useful to be able to build strings from numerical values in your script. This need often arises in formatting printout of results to look nice, or in generating filenames. Suppose `a = 2` and `b = 3`. Then, the following example show how you can insert the values into a string:

```python
s = '%d + %d = %d' %(a,b,a+b)
print s
```

note that the "input" to the format string must be a `tuple`, not a list; recall, however, that if `L` is a list, the function call `tuple(L)` will return a tuple whose elements are those of the list input as the argument. If the tuple has only one element, you can leave off the parentheses. The format code `%d` (or equivalently `%i`) converts an integer into a string. You use `%f` for floating point numbers, and `%e` for floats in scientific notation. There are other options to these format codes which give you more control over the appearance of the output, and also several additional format codes.

Now make up a few examples of your own and try them out.

### 2.1.3 Modules

To do almost any useful science with Python, you will need to load various libraries, known as "modules." Actually, a module can be just an ordinary Python script, which defines various functions and other things that are not provided by the core language. A module can also provide access to high-performance extensions written using compiled languages.

To make use of a module with name `myModule`, you just type: `import myModule`. Members of the module are accessed by prepending the module name to the member name, separated by a ".". For example, if `myModule` contains the constant `r_earth` and the function `sza`, these constant is accessed using `myModule.r_earth` and the function is evaluated at `t` using `myModule.sza(t)`. If you don’t need to keep the module’s members separate, you can avoid the need of prepending the module name by using `from myModule import *`.

The standard math functions are in the module `math`, and you make them available by typing `import math`. To see what’s there, type `dir(math)`; this works for any module. Now, to compute `sin(\pi/7)` for example, you type `math.sin(math.pi/7.)`. To find out more about the function `math.sin`, just type `help(math.sin)`. If you don’t like typing `math.sin`, you can import the module using `from math import *` instead, and then you can just use `sin, cos, etc. without the prefix.`

### 2.1.4 Getting help

Python has extensive built-in help functions, which make it possible to learn new things and avoid programming errors without frequent recourse to manuals. Given that so much of Python is found in various language extensions the Python community has written, the availability of embedded documentation is beholden to the good behavior of the programmer. Python fosters a culture of
good behavior, and tries to make it easy for developers to provide ample help and documentation integrated with the tools they have developed.

The main ways of getting help in Python are the help() and dir() functions. For example, you have learned about the split() method that is one of the methods available to strings. Suppose you didn’t know what methods or data attributes went along with a string, though? Rather than going to a handbook, you can use the dir() function to find out this sort of thing. For example, if a is a string, you can type dir(a) to get a list of all its methods, and also all its data attributes (e.g. its length). Then, if you want to know more about the split() method you can type help(a.split) (Warning: don’t type help(a.split()), which would look for help items on the words in the content of the string!). Both strings and lists have many useful and powerful methods attached to them. Many of these will be illustrated in the course of the examples given in the rest of this Workbook, but you are encouraged to explore them on your own, by finding out about them using dir() and help(), and then trying them out.

So when in doubt, try help and dir. One or the other will give you some useful information about just about anything in Python. If the system you are working on has the Python HTML documentation files installed, you can even get help on Python syntax and Python key words online. For example, to find out what the Python keyword for means, you just type help("for").

Further, since Python is interpreted rather than compiled into machine language, if you have some Python programs written by somebody else, you can almost always “look under the hood” to see how they work. That is not generally possible with compiled languages where you often don’t have access to the original source code.

### 2.1.5 Program control: Looping, conditionals and functions

Now we’re ready for some more involved programming constructions. The basic technique for writing a loop is illustrated by the following example, which prints out the integers from 0 through 9:

```python
for i in range(10):
    x = i*i
    print i, x
```

Note that in Python, indentation is part of the syntax. In the above example, the indentation is the only way Python has to identify the block of instructions that is being looped over. Indentation in a block of code must line up, and you need to be cautious not to confuse spaces and tabs. The use of indentation as a syntactic element in Python enforces code readability and reduces the need for special identifiers to terminate blocks.

The construct range(10) is actually shorthand for the 10-element list

\[0,1,2,3,4,5,6,7,8,9\]

In fact, one of Python’s many charms is that a for loop can loop over the elements of any list at all, regardless of what the elements of the list may be. Thus, the following example sums up the length of four strings:

```python
myList = ['bob','carol','ted','alice']
n = 0
```
for name in myList:
    n = n + len(name)

This can be very useful for looping over file names with data needing to be processed, or data arrays which need something done to them, and all sorts of other things that will occur to you once you get accustomed to the concept.

An alternate to looping over a list is to use the while construction, as in:

```python
x = 1.
while x < 100.:
    print x
    x = 1.1*x
```

Now, for practice, write a loop to compute 52 factorial (i.e. $52 \times 51 \times \ldots \times 1$). Note that Python automatically starts using long integers when it needs to.

In doing computations, it is typical that one needs to test for the satisfaction of a condition at some point before proceeding. For example, one might need to test whether a temperature is below or above freezing to decide whether to form ice or liquid water. Programming languages generally provide some conditional control to handle this situation, and Python is no exception. The following illustrates the use of an if block in Python:

```python
if T < 273.15:
    print "Too cold!"

and an extended if block:

```python
if T < 273.15:
    print "Too cold!"
elif T > 373.15:
    print "Too hot!"
else:
    print "Just right!"
```  

An if block can have as many elif blocks as you need, and the conditional being tested can be anything that reasonably evaluates to a truth value. To distinguish from assignment, the equality relation is expressed by the symbol ==. The symbols <= and >= have the obvious meanings. The exclamation point negates a relation, and Python also provides the operator not to negate the truth value of an arbitrary logical expression. For example 1 != 0 and not (1 == 0) mean the same thing. Compound expressions can be built up from the Boolean operators for "and" (&) and "or" (|, the vertical bar). Python also provides the keywords True and False for logical values, but regular integers 1 and 0 generally do just as well in conditionals.

The organization of almost any program can benefit from the subdivision of the labor of the program into a number of functions. This makes the program easier to debug, since functions can be tested individually. It also allows the re-use of code that is needed in many different places in the program. The basic means of defining a function is illustrated in the following example, which returns the square of the argument:

```python
def f(x):
    return x*x
```
2.1. *FUN WITH PYTHON*

From the command line, you would invoke this function, once it is defined, by typing, e.g. `f(3)`.

Python can even handle recursion in functions. That is, functions can be defined in terms of themselves. As an example, a function to compute the factorial of `n` could be written:

```python
def factorial(n):
    if n == 0:
        return 1
    else:
        return n*factorial(n-1)
```

Functions can return multiple arguments, as in:

```python
def powers(x):
    return x,x*x,x*x*x
```

This returns a tuple containing the three values. It can be very nicely used with Python’s ability to set multiple items to corresponding items of a tuple, using constructions of the form:

```python
x1,x2,x3 = powers(2)
```

Python functions work only on a *copy* of the arguments. It is important to keep this in mind, since it means that any changes made to these arguments (“side-effects”) do not affect the variable’s value in the calling program. Try this:

```python
def f(myValue):
    myValue = 0
    x = 1
    print x
    f(x)
    print x
```

In this example, `x` is unchanged because functions work only on a local copy of their arguments. However, if the argument is a name which points to the location of some data, the data pointed to can be modified in the function. This may seem somewhat arcane, but the following simple example modifying an element in a list should illustrate the general principle:

```python
def f(myList):
    myList[0] = myList[1]

L = [1,2,3,4,5]
f(L)
print L
```

If you want to replace the list with a completely new list, based on the old one, the right way to do this is to return the new list, rather than doing anything to the argument:

```python
def bump(myList):
```
newList = [ ]
for item in myList:
    newList.append(item+1)
return newList

Then, if the user really intended to replace the old list, he or she would use L = bump(L)

Often, the evaluation of a function will require a number of constants or parameters which
you might not need to change very often, or which are common to a great many different functions.
These could always be added to the parameter list. If there are many of them, that could become
tedious. Soon you will learn how to create objects which provide a way to package data in a
way that allows you to keep the argument list of functions under control. There is yet another
technique, though, that can be useful if used with discretion, namely the global variable.

Global variables are set outside functions, and can be accessed by any function that needs
them. In many languages, global variables need to be declared explicitly, but Python simply makes
an intelligent guess about what you intend to be global. Basically, if a variable is used within a
function, but is neither set in the function nor is in the argument list, Python assumes it to be
global. Note that the same variable name can be local in one function (if it is set internally), but
global in another. As an example of the use of global variables, consider the function computing
the acceleration of gravity towards the center of a planet at the origin:

    def grav(r):
        return -G*M/(r*r)

This has a problem, because the gravitational constant G and the mass of the planet M have not
been defined anywhere. It’s bad practice to hard-wire their values in the function, because then
it’s inconvenient to change them later. If you try evaluating the function after you’ve defined it,
you’ll get an error message (try it). However, if you type:

    G = 6.6742e-11 # In mks units
    M = 6.4185e23 #Mass of Mars in kg
    grav(1.e12)

everything will work fine. You do not need to define the globals until you want to evaluate the
function, and you can change their values at any time.

This is convenient, but if you have too many globals being set in too many places, it can
be hard to keep track of what is going on. It is also bad practice to use globals for things you will
change a lot, which would more appropriately be arguments. The behavior of globals can become
even more confusing if you have functions spread across several different files. Nonetheless, you
will encounter many cases where using a few globals does the job nicely.

2.2 More advanced Python

Having covered the basics, we now introduce some Python techniques that will be of use in writing
programs to do more complex tasks. This is fairly optional material for beginners interested pri-
marily in scientific computation, so the reader may wish to skip ahead to the section on Courseware
modules, perhaps pausing on the way to take a look at the section on the numpy array module.
2.2. MORE ADVANCED PYTHON

2.2.1 Writing your own modules and executable scripts

A module should be thought of as a library of useful definitions, including values of constants, lists, definitions of functions, objects, definition of object types, and what have you. A module can also contain executable commands of any type, which are executed by the interpreter when the module is imported. In fact, Python doesn’t make any real distinction between a module and any other executable script. Generally, you should think of modules as a place to store things that you will use repeatedly. Although you can execute a module any way that a Python script can usually be executed, a module is intended to be used by importing it into some other script that needs the entities defined by the module.

Generally, when developing code in Python, you always have an interpreter window open and an idle editor window. You try things out in the interpreter window, and if things work, you move things into the editor window, which you save for use as an executable script or as a module.

Let’s say that you’ve written a Python script and saved it as myModule.py. This script might execute a bunch of calculations, or it might just define functions that you want to use interactively from the Python command line, or it might do both. You can run this Python script from within the Python interpreter by typing import myModule. This will run all the executable statements, and also load any functions and so forth that you’ve defined in your file. This way of running is especially useful if you’ve defined a lot of nifty functions in your file, and then want to load them in so that you can try them out interactively in the interpreter. Note that all variables and functions imported in this way must be referred to with myModule. stuck on the beginning of it’s name. Thus, if your file had the statement radius = 6.0e6 in it, once you imported the file, you would use myModule.radius to get at the value of radius. Suppose now that you want to change the Python program you’ve just tried out. For example, you might want to change the definition of the radius to radius = 6.0e07. You can edit myModule.py in the editor window and save it, but to get the interpreter to recognize the changes, it doesn’t work to simply import it again. Instead, you need to type reload(myModule) into the interpreter.

You can import many different scripts into your Python interpreter session, and also use the import command in scripts you write yourself. Indeed, this is the way that extensions to Python are handled.

If you’ve written a script that performs some one task (e.g. making a plot of a temperature profile), it is not good practice to execute it by importing it as a module. Rather, you should save the file (say, myprog.py), then execute it from the command line by typing python myprog.py, or by loading it into an editor window in idle and executing it from there.

2.2.2 List comprehension

List comprehension refers to the ability to create new lists by processing elements of old lists. It is one of the powerful features of Python that allows one to write compact, readable code, often doing without multiline loops. As a simple example, say we want to generate a list of 10 real numbers equally spaced by increments of 1. Instead of writing a for loop and appending the values to a list, one can simply write [.1*i for i in range(10)]. Combined with the ability of Python to loop over any list at all, this is very versatile. For example, one can write [ f(.1) for f in [math.sin,math.cos,math.exp]]. Suppose we have an averaging function avg which returns the average of the elements of a list. Then, if L is a list of lists we want to average, we can create a list of average values by writing [avg(list) for list in L] The power of list comprehension is further enhanced by Python’s ability to do multiple assignments on a single line. For example,
suppose we want to open three files, with names data0, data1, and data2. This can be done on a single line using

```python
file0,file1,file2 = [open(name) for name in ['data%d' % i for i in range(3)]]
```

The `open` statement which appears in this example is a built-in Python function that opens a file and returns a file object that can be used to read the contents of the file, or write new contents to the file.

### 2.2.3 Using objects in Python

An object is a collection of data and functions that act on the data. The functions in an object are known as methods. Almost everything in Python is an object, and you have in fact been working with many objects all along. For example, if `mystring = 'Use the force!'`, then when you split it using `mystring.split()` you are invoking the `split` method of a string object. The elements of an object are referenced by separating the name of the object from the element by a period, as in the string example. A method of an object is called with parentheses, like any other function. In the string splitting example, the method was called without any arguments, because the argument of the `split()` method is optional. In fact this method can take an argument, which is the character you want to use for splitting the string. Try `mystring.split('e')` to see what happens (in practice, it would be more common to split on characters like a comma or the special tab-key character, represented by '⁀'). Objects can have data values stored in them as well, and these are referred to in a way similar to methods, but without parentheses. The string object has only methods and no data values, but the complex number object provides a good example. For example if `z = 2+3j`, then `z.real` gives you the real part and `z.imag` gives you the imaginary part. Compare this with the method `z.conjugate()`, which returns the complex conjugate of `z`. Objects can, if the designer so provides, do many other things. Objects can be called like functions. They can be indexed like lists or arrays (as in `myobject['frodo']`), and they can even be used in arithmetic expressions.

The designer of an object does not actually define the object itself. The designer defines a class of objects. When you use an object, you create an instance of the object, just like an individual guinea pig is an instance of the general type of object known as GuineaPig. Suppose somebody has defined a class GuineaPig, which when instantiated has to be given a name and a weight in kilograms. Type in the following lines to define a GuineaPig class. You may be able to guess what some of the lines mean, but don’t worry about details for now; we’ll go into the definition of classes in more detail later.

```python
class GuineaPig:
    def __init__(self,piggyName,piggyWeight):
        self.name = piggyName
        self.weight = piggyWeight
    def purr(self):
        print "purrrrrrrr"
    def squeak(self,squeakType):
        if squeakType == "loud":
            print "SQUEAK!!!!"
        elif squeakType == "soft":
            print "squeak"
```
elif squeakType == "slow":
    print "s q u e a k"
else:
    print "Week! Week! Week!"

def eat(self):
    self.weight = self.weight + .1

Once you have defined the GuineaPig class, you create an instance by typing `myPiggy = GuineaPig("Fluffy", 1.2)`. Thereafter, you can get the weight by typing `myPiggy.weight` and the name by `myPiggy.name`. The object might also have various methods, such as `myPiggy.squeak("loud")`, or `myPiggy.purr()` or `myPiggy.eat()`. The `eat` method might do something like increment the weight when it is called. You can create as many GuineaPig objects as you like, and each will keep track of the data belonging to itself. Try creating a few GuineaPigs with different names and initial weights. Make a few of them eat, then check their weight.

In Python, objects can be dynamically modified. That means that new data elements can be added to an existing instance of an object at any time. This can be very handy for packaging up functions and parameters for handing off as an argument to another function. The following example shows how you can create an object with the gravitational constant, the mass of the Mars, and a function as members. It does this by first creating an instance of the class Dummy whose instances have nothing in them (the Python statement `pass` means simply "do nothing"). Then creating an instance of the class, called info, and adding some data elements to the instance dynamically.

```python
# Define the class
class Dummy:
    pass

# Make an instance and then stick in some data elements
info = Dummy()
info.G = 6.6742e-11
info.M = 6.4185e23

# Define a function
#
# def f(x):
#     return x/(1. + x)
#
# Stick in the function as a new data element. Note that as far as Python is concerned, a function name is like any other data name. These data names can represent numbers, complex numbers, lists, other objects, functions, whatever.
# info.function = f

The following shows how you might define a function using this information:

def g(r, input):
    return input.G * input.M * input.function(r)/r**2

You would call this function with a statement like `g(1.e7, info)`. Try it.

This brief discussion is intended to provide enough background to allow you to work with classes others have defined. The usage of objects will become clearer as you gain more experience.
working with them. In the Advanced Topics section to follow, we will take up the matter of designing your own objects.

2.3 The numpy array module

Lists look like arrays, and are versatile objects, but they are not very efficient at fulfilling the functions one expects of the kind of arrays that appear in moderate to large scale scientific computation. It would be possible to write a 2D matrix as a list of lists, and even implement matrix multiplication and vector addition for such an object. However, it would be very inefficient, because lists provide for a very general and mutable data structure. Python does have a native array data type, which is somewhat more efficient, but is still not very good for scientific computing.

This is where the real power of the extensibility feature of Python comes in. When the language is missing some feature some community really needs, the community gets together and writes an extension module which fills the bill. Sometimes this is a cooperative process. Sometimes it is an evolutionary process, with many competing extensions co-existing until one comes to dominate. For scientific arrays, the solution that has come to the fore is the numpy module, which provides highly efficient Matlab-style array objects. This purpose was earlier served by the older Numeric module, which may still be found in some older installations. From the standpoint of the user, almost all of the array manipulations are the same between Numeric and numpy. numpy is not written in Python. It is written in very highly optimized c++, which is why it is so efficient. This does not mean the developers of numpy had to learn a lot about the internal structure of Python or spend much time at all turning their compiled library of objects into commands that could be accessed within Python. In fact, once such a library is developed, it can be turned into a Python module more or less automatically using a preprocessor known as swig (see swig.org for more details). Compiled FORTRAN libraries can be similarly spliced into Python using pyfort or f2py. For this reason, a great variety of numerical analysis libraries are already available as Python modules. Moreover, if you know how to program in c, c++ or FORTRAN, you can very easily learn to build your own customized Python modules. The general strategy is to do as little as possible at the compiled level, building tools there that are very general and of broad applicability. One seeks to isolate the computationally intensive work in a few compiled toolkits, and build more complex models out of these building blocks at the Python level.

numpy provides one of the most fundamental building blocks for scientific programming in Python, and most other Python modules doing numerical analysis or data analysis deal with numpy arrays. The numpy module is imported like any other module, using import numpy. numpy arrays can have however many dimensions you need.

The first step in using a numpy array is to create it. numpy provides various ways to do this. To create an array, you need to specify its dimensions and its datatype. Commonly used data types are default float (numpy.float, usually double precision), default complex (numpy.Complex), and default integer (numpy.int, typically a 32-bit int). (The old Numeric module uses upper case Int, Float, etc. for these). numpy does not currently support 64-bit integers unless they are the default integer type on the machine you are using. It also does not support the unlimited precision Python integers, though other modules are available which do. Dimensions are specified as a tuple or a list of integers. For example, the dimensions of a 3 by 5 array are specified as (3,5) or [3,5]. If the array is one-dimensional, you can just use an integer in place of a list or tuple, if you wish.

One way to create an array in Python is to call a creation routine which makes an array of the desired dimension and fills it in with default data of some particular type. For example, the
following lines create a 5 by 10 floating point array of zeroes, a one-dimensional integer array of ones of length 100, and a 10 by 10 complex identity matrix. You can see the values of an array, if it is not too big, by just typing its name.

```python
A = numpy.zeros((5,10),numpy.float)
B = numpy.ones(100,numpy.int)
C = numpy.identity(10, Numeric.complex)
```

A typical thing to do would be to create an array of zeroes, then fill in the values you want in a loop, as in:

```python
A = numpy.zeros((5,10),numpy.float)
for i in range(5):
    for j in range(10):
```

This example also illustrates the way one refers to elements of an array in Python. Python arrays are zero-based, i.e. \( A[0,0] \) is the first element in the case above. The designers of `numpy` provided a very versatile indexing handler, so in fact you could equally well refer to the \( i,j \) element as \( A[i][j] \). In essence, multidimensional `numpy` arrays act like a list of lists. We’ll return to this shortly, in our discussion of array cross section notation. Another important thing to know about `numpy` array indexing is that it conforms to Python list usage with regard to negative numbers. For example, if \( B \) is a one-dimensional array, \( B[-1] \) is the last element of the array, \( B[-2] \) is the next to last, and so forth. Try this with a 2D array, to make sure you understand the indexing convention.

An array can also be created from a list. You can let `numpy` infer the data type from the contents of the list, or you can specify it explicitly, in which case a conversion is performed. Try the following statements, and see what kind of array is produced:

```python
A = numpy.array([.1,.2,.3])
B = numpy.array(range(20),numpy.complex)
C = numpy.array( [[1.,2.],[-2.,1.]] )
```

Another useful way to create an array is to define it in terms of a function on the indices, so \( A[i,j] = f(i,j) \), \( f \) being some function you have defined. This is probably the most common way of creating the kind of array used in scientific computation without employing a loop. It will generally operate much faster than a Python loop, especially for large arrays. The following illustrates how to create a 10 by 10 array from a function:

```python
dx = .1
dy = .2
def f(i,j):
    x = dx*i
    y = dy*j
    return x*x + y*y
A = numpy.fromfunction(f,(10,10))
```

The two parameters \( dx \) and \( dy \) are provided to the function \( f \) as globals, because that is the only way `numpy` has provided to pass auxiliary information to the function defining the array. There
is an important subtlety in the use of `fromfunction`. The parameters `i` and `j` look like integers, but in fact they are arrays of the same dimension as the array being created. The above example works because the arithmetic being done on the arguments is actually array arithmetic. This allows `fromfunction` to call the function only a single time, rather than in a loop, and results in a much faster computation. If you are using other functions or list indexing inside your creation function, you must take this into account. For example, the following code will work:

```python
dx = .1
dy = .2
def f(i,j):
    x = dx*i
    y = dy*j
    return numpy.sin(x)*numpy.sin(y)
A = numpy.fromfunction(f,(10,10))
```

but if we used `math.sin` and `math.cos` instead, it would not work, since these functions do not operate on and return `numpy` arrays. Similarly, an expression like `myList[i]` will not work inside the function `f` since `i` is not an integer, and so can’t be used as an index. There are workarounds, but generally speaking, `fromfunction` does not work very gracefully with table look-up operations. If you are still confused about just what `i` and `j` are, try putting a print statement in the function to print out the arguments.

There are other ways to create arrays, but the above methods should take care of any cases you are likely to encounter. We have already illustrated how to refer to individual array elements, but it is worth knowing about some of the powerful `array cross section` indexing features allowed by `numpy`, which allow you to refer to subarrays easily. Python uses the colon (`:`) as an identifier to build cross sections. The colon by itself stands for the full range of values of the corresponding index. For example, if `A` is a 5 by 5 array, the subarray `A[:,0]` is the one dimensional array with elements `A[0,0], A[1,0], ..., A[4,0]`. An index of the form `m:n` would denote the range of values `m,m+1,...,n-1`, so that `A[1:3,0]` would be the array with elements `A[1,0], A[2,0]`. If you leave off one of the endpoints, Python substitutes the first array element for the starting point, or the final array element for the ending point. If `B` were a 100 element array, for example, `B[:25]` would be the same as `B[0:25]` and `B[50:]` would be the same as `B[50:100]`. Finally, you can specify a stride, allowing you to pick off every `k`th element. Thus, `0:10:3` represents the set of indices `0,3,6,9`. You can combine subarray indices for the various dimensions of an array in any way you want, as in `A[0:8:2,5:]`.

Now we come to the most powerful aspect of `numpy` arrays, namely that one can do arithmetic with them just as if they were scalars, avoiding the writing of inefficient and cumbersome loops. The following statements illustrate the kind of arithmentic operations that can be performed with arrays. Note that you will get an error if you try to perform arithmetic on incompatibly sized arrays (e.g. adding a 10 by 10 array to a 5 by 5 array).

```python
A = numpy.ones((10,10),numpy.float)
B = numpy.identity(10,numpy.float)
C = (A-B)*10. #You can multiply by a scalar
C1 = (A-B)*B  #You can multiply by an array
D = A/(A+2) #You can divide arrays.
E = C**5.2  #Exponentiation
```

The expressions can be as complicated as you want. Note that `numpy` array multiplication is
element-by-element multiplication, rather than matrix multiplication (and similarly for division). If you want matrix multiplication you use the `numpy.dot(...)` function, as in `C = numpy.dot(A, A)`. When the two arrays are 1D, this reduces to the conventional vector dot product. There is also a function `numpy.outerproduct` which computes the outer product of two arrays. `numpy` does not provide a function for matrix inversion; that can be found in various other linear algebra packages made to work on `numpy` arrays.

`numpy` also provides versions of the standard math functions, that work on entire arrays. For example `B = numpy.sin(A)` returns an array of the same dimension as `A`, whose elements are the sin of the corresponding elements of `A`.

Array arithmetic can be done between arrays of different types, if the operation makes sense. The result is promoted to the higher of the two operands. For example, adding an integer and a complex results in a complex, or adding a single precision float to a double precision float yields a double precision float. The default float type for `numpy` arrays is double precision. All floating point scalars in Python are also treated as double precision, so an operation involving a Python float constant and a `numpy` float array will yield a double precision array.

Cross sections can be used with array arithmetic to compute many useful derived quantities without the need of writing loops. For example, an approximation to the derivative of a function whose values at an array of points `x` are tabulated in the array `F` (i.e. `F[j] = f(x[j])`) can be computed using:

```python
# We assume the function f and the array x have been defined already
F = numpy.array([f(x1) for x1 in x])
n = len(x)
dx = x[1:n]-x[0:(n-1)]
df = F[1:n]-F[0:(n-1)]
dfdx = df/dx
xmid = (x[1:n]+x[0:(n-1)])/2.
```

The final line defines the array of midpoints, where the derivative has been estimated. Note the use of list comprehension to generate the array `F`. Array cross sections can also be used to do matrix row and column operations efficiently. For example, suppose `A` is an n by n matrix. Then a set of row and column reductions can be done with the following 1D loop:

```python
for i in range(n):
    A[:,i] = A[:,i] - 3.*A[:,0]
```

You can even do a fairly broad class of conditional operations on arrays, using the `numpy.where` function. This function takes three arguments. The first is a conditional involving an array. The second is an array expression, to be evaluated and returned if the conditional is satisfied. The third argument is the expression to be returned if the conditional is not satisfied. For example, the following use of `where` returns the array `A` where `B` is negative, and returns the value 1. where `B` is non-negative:

```python
C = numpy.where(B<0, A, 1)
```

Note that the array `A` must have the same dimensions as `B`, since the conditional is evaluated element-by-element. The expressions can be quite complicated. For example:
The combination of array cross sections, conditionals and array arithmetic is so powerful that one should only rarely need to resort to writing a loop. This is a good thing, since large loops run very slowly in Python, as in other interpreted languages. Try computing the matrix product of two 200 by 200 arrays using an explicit loop, and compare to the time taken to do the same multiplication using `numpy.dot`. Avoiding loops is also good practice because it makes the meaning of your code more transparent.

`numpy` offers a rich variety of other useful array operations, such as convolution. For additional information on `numpy`, just type `help(numpy)` after you’ve imported it. Full documentation can be found at http://docs.scipy.org/doc/.

### 2.4 Courseware modules

These are modules that I have written myself, as an aid to using Python for research and teaching in various areas of the physical sciences. The special emphasis is on planetary climate, but these modules are broadly useful. They are currently distributed via the *Principles of Planetary Climate* web site.

#### 2.4.1 The `ClimateUtilities` module

The `ClimateUtilities` module is a general-purpose collection of input-output, graphical and numerical analysis routines, plus definition of some useful object classes. Highlights of the contents of this module are given below.

**The Curve object and its uses**

The `ClimateUtilities` module written for use with this course provides a `Curve` object, which is intended to simplify the process of reading, and writing plain-text tabular data, and of plotting data which has either been read in from a file or generated by some calculation in your script. In essence, a `Curve` object is a set of data columns, each of which must be the same length, together with optional auxiliary information describing the data. The auxiliary information also allows you to specify certain things about how the data will look when it is plotted.

To use a `Curve` object, you create one, and then ”install” data columns using the `addCurve(...)` method. Since `Curve` objects are intended to represent data sets in which any element of a column can be regarded as a function of the corresponding element of another column, all data columns installed must have the same length. You can install any one-dimensional indexable object, including lists and `numpy` arrays. If you install a list, it will be converted automatically to a `numpy` array, so you can do arithmetic with it.

The following example creates a curve object containing values of $x$, $\sin(x)$ and $\cos(x)$.

```python
c = [i/10. for i in range(101)]
y1 = [math.sin(xx) for xx in x]
y2 = [math.cos(xx) for xx in x]
```

```python
c = numpy.where(numpy.sin(B)>0, numpy.exp(1.+ B*B),numpy.exp(1.-B*B))
```
y2 = [math.cos(xx) for xx in x]
c = Curve()
c.addCurve(x,'x','x axis label')
c.addCurve(y1,'y1','sin(x)')
c.addCurve(y2,'y2','cos(x)')

The first argument is mandatory, since it defines the data you want to install in the Curve. The second argument of addCurve defines a variable name, which you will use to refer to that data column. It is optional. If you omit it, the Curve object will create a variable name of the form v0,v1,v2,... If you specify a variable name yourself, you can also optionally specify a "long name," or label, which is used to label the corresponding data when plotting, and also to provide more long-winded information about what the variable represents. The label can be a good place to record the units of a variable.

Curve objects are indexed. You refer to a data column by its variable name. In the above example, c['x'] returns a numpy array of the x column, and c['x'][30] would return item 30 of that array. You can get a list of variable names in a Curve object by using the listVariables method, as in c.listVariables()

Since data in a Curve object is stored in the form of a numpy array, you can do arithmetic on the data directly. For example

prod = c['y1']*c['y2']

creates a new array prod containing the product of each element of the array c['y1'] with the corresponding element of the array c['y2']. You can even use arithmetic to transform data in-place, or even to create new columns in the Curve object, as illustrated in the following:

c['y2'] = 2.*c['y2'] + 7.
c['y2'] = numpy.log(c['y2']) #You must use numpy array functions for arrays
c['sum'] = c['y1']+c['y2']

A good general technique for putting data from a calculation into a Curve object for saving, plotting or further analysis is to accumulate the data into a set of lists, and then install the lists in a Curve object. This way, there is no need to know in advance how long the data objects will be. When data from a list is installed in a Curve object it is automatically converted to a numpy array. The following code snippet provides an example:

xlist = []
ylist = []
x = 1.
xfact = 1.1
while x < 100.:  
    xlist.append(x)
    ylist.append(x*x)
    x = x*1.1 # or, equivalently x *= 1.1

c = Curve()
c.addCurve(xlist,'x')
c.addCurve(ylist,'y')
The **ReadTable(...)** function

The `readTable(...)` function in `ClimateUtilities` will read columnar tab or space-delimited data from a text file and return a `Curve` object with the data. It is called with the filename as the argument; for example to read the file "profile.txt", you would type `c = readTable("profile.txt")`. The filename can also contain the path to the directory where the data is located, if necessary. Note that you do not have to create the `Curve` object yourself; that is done for you by the `readTable` function. If the data set contains column headers containing variable names (without spaces or tabs in them), `readTable` will recognize that and use them as variable names. `readTable` will also do a pretty smart job of recognizing what is data and what is text description of the data set, such as often is found at the beginning or end of a file. Descriptive text will be separated out from the data, and returned as the `description` element of the `Curve` object.

The **plot(...)** function

`ClimateUtilities` also provides an easy-to-use `plot` function which produces line graphs from `Curve` objects. One of the data columns must be designated as the independent, or "x" axis; other data will be plotted as a function of this. By default, the first column installed is designated the "x" axis, but any other curve can be so designated using the `Xid` element (e.g. `c.Xid = 'y1'` in the above example.

If you want to plot the data in a `Curve` object `c`, you can simply type `plot(c)`. The `Curve` object has the following plot options, which can be set to control the appearance of the plot. If `c` is the `Curve` object, then:

- `c.XlogAxis = True` plots the x axis with a log scale, and similarly for `c.YlogAxis`.
- `c.reverseX = True` plots the x axis data with the largest values at the left, and `c.reverseY` plots the y axis data with the largest values at the bottom.
- `c.switchXY = True` switches the x and y axes. For example if you are plotting temperature `T` as a function of pressure `p` (which is designated as the x axis) and you want to make the pressure appear on the vertical axis, you would invoke this option. If you are just plotting one column, the same effect could be achieved by just changing the specification `c.Xid`, but if you are plotting multiple curves on the same graph, you would need to use the `c.switchXY` option.
- If you want any data column to be plotted as a scatter plot, i.e. with symbols at the data points but no line drawn, you can set `c.scatter(varname) = True`, where `varname` is the name of the variable you wish to affect – for example, "y1" in the sin and cos curve we defined earlier.

When you call `plot` it puts up the plot in a window which you can move around, but which you won’t be able to get rid of until you terminate the Python shell. `plot` actually returns a plot object which you can use to do further things with the plot. In particular, if you were to write `w = plot(c)`, then you can make use of the plot object `w`. For example `w.delete()` gets rid of the plot window. You can also use the plot object to save the plot as a postscript file, for later printing or incorporating into a lab report. You do this by typing `w.save('myplot')`, which save the plot into the file `myplot.ps`. You can of course replace the filename `myplot` with whatever name you want.
If you don’t want to use the python-based graphics, you can always use `c.dump('myfile.txt')` which makes a tab-delimited text file, and then plot it using the program of your choice.

**Numerical analysis routines in ClimateUtilities**

### 2.4.2 The `phys` module

### 2.4.3 The `planets` module

## 2.5 Advanced Python Topics

### 2.5.1 Defining your own objects

You define a new type of object by using the `class` statement. This will define the data and functions (known as “methods”) that will be part of the object. The `class` statement should specify a special method called `__init__(...)` which is known as a *constructor*. This method is invoked when a new instance of the object is created, and says what needs to be done to create the object. Sometimes the creation process is very simple, but the creation process can also be very complex. Certain methods, like `__init__`, have special meaning. All such methods have names with begin and end with a double underscore.

As a simple example, the following class defines an object which can be used to evaluate the gravitational acceleration as a function of distance to a planet with mass M:

```python
class gravity:
    def __init__(self,M,G):
        self.M = M
        self.G = G
    def accel(self,r):
        return -self.G*self.M/(r*r)
```

The argument `self` must be the first argument to every method defined in the object. It provides a way to refer to the members of the particular instance of the object being worked on. When you actually call the methods, or create the object, you leave off the `self` argument and Python puts it in automatically. To make an object of the type we have just defined, and use it to compute the acceleration at a certain distance, you would use

```python
g = gravity(6.4185e23,6.6742e-11) #Invokes the __init__ method to create an
#instance of a gravity object
```

```python
g.accel(1.e12) #Computes the acceleration
```

You can improve the object by making it callable, so it acts just like a function. You do this by adding a `__call__` method:

```python
class gravity:
    def __init__(self,M,G):
        self.M = M
        self.G = G
    def __call__(self,r):
        return -self.G*self.M/(r*r)
```

```python
g(1.e12) #Computes the acceleration
```
def __call__(self,r):
    return self.accel(r)

def accel(self,r):
    return -self.G*self.M/(r*r)

If you create an instance \( g \) of this object, the acceleration can be computed by just typing \( g(r) \). This is a convenient technique for creating functions that remember the parameters needed to compute themselves.

Now, since the gravitational constant is a *universal constant* which should never change from one planet to another, it is rather silly to have to specify it separately for each planet. Python objects allow you to specify data that is common to all objects of a given type. If this class data is changed somewhere, the change applies to all objects. This behavior is useful not just for shared constants, but also provides a way for one instance of an object to communicate with all other instances of an the same kind of object. Class data is specified within the class definition without any identifier. It is referred to using the name of the class, rather than the name of an instance. The following example re-implements the class, making \( G \) into class data, and also implementing a class-level counter that keeps track of the number of planets created:

class gravity:
    G = 6.6742e-11
    nPlanets = 0
    def __init__(self,M):
        self.M = M
        gravity.nPlanets = gravity.nPlanets + 1
    def __call__(self,r):
        return self.accel(r)
    def accel(self,r):
        return -gravity.G*self.M/(r*r)

Now, you can create two planets using \( \text{planet1} = \text{gravity}(6.4\text{e}23) \) and \( \text{planet2} = \text{gravity12.e}23 \). The two masses are still \( \text{planet1}.M \) and \( \text{planet2}.M \), and you compute the gravity for the two planets using \( \text{planet1}(1.\text{e}6) \) and \( \text{planet2}(1.\text{e}6) \) as before. Now, however, if you need to change the value of the gravitational constant, you can update it for all the planets by writing, for example, \( \text{gravity}.G = 6.672\text{e}11 \). At any time, the number of gravity objects instantiated so far will be \( \text{gravity}.nPlanets \). In many applications, an object will store data in the form of arrays. In such cases, the \_init\_ method typically will create the arrays and set their initial value. For example, the following class creates and initializes pressure and temperature arrays of a specified length:

class profile:
    def __init__(self,n,p0,T0):
        self.p = numpy.array(range(n),numpy.float)*p0/(n-1)
        self.T = numpy.ones(n)*T0
    def warm(self,dT):
        self.T = self.T + dT

The class provides a method which increments the temperature by an amount \( dT \). Once you have imported \texttt{numpy}, you can create an instance using \( \text{pT1} = \text{profile}(100,1000.,300.) \). If you want...
to find the pressure at index 4, you would type `pT1.p[4]`, and similarly for temperature. You can also change the values of the arrays as you would for any other `numpy` array, using, e.g. `pT1.T[10] = 301.`.

The special methods `__getitem__` and `__setitem__` allow you to make an object indexable, so that individual elements of an object can be retrieved by specifying an index of some type. Array elements are indexed by specifying sequences of integers, but the object used for doing the indexing can be quite general. The following example shows how to make and use a tridiagonal array object, which can be addressed as if it were a full matrix.

class tridiag:
    def __init__(self,n):
        self.A = numpy.zeros(n,numpy.float)
        self.B = numpy.zeros(n,numpy.float)
        self.C = numpy.zeros(n,numpy.float)
    def __getitem__(self,key):
        # key is a list of arguments passed within square
        # brackets when an indexing operation is performed
        # on an instance of the object. In this case,
        # key is expected to be a two element list.
        if key[0] < key[1] - 1:
            return 0.
        if key[0] > key[1] + 1:
            return 0.
        if key[0] == key[1] -1:
            return self.A[key[1]] #Below the diagonal case
        if key[0] == key[1]:
            return self.B[key[1]] #Diagonal case
        if key[0] == key[1]+1:
            return self.C[key[1]] #Above the diagonal case
    def __setitem__(self,key,value):
        # key is a list of arguments passed within square
        # brackets when an indexing operation is performed
        # on an instance of the object. In this case,
        # key is expected to be a two element list.
        #
        # value is the value to which the element is to be set.
        # It is taken from the right hand side of the equal
        # sign in an expression like M[i,j] = 1., where M
        # is an instance of the object.
        #
        if key[0] < key[1] - 1:
            print "Out of bounds"
        if key[0] > key[1] + 1:
            print "Out of bounds"
        if key[0] == key[1] -1:
            self.A[key[1]] = value #Below the diagonal case
        if key[0] == key[1]:
            self.B[key[1]] = value #Diagonal case
        if key[0] == key[1]+1:
The object could be used as follows:

```python
M = tridiag(10)
for i in range(10):
    M[i-1,i] = 1.
    M[i,i] = -2.
    M[i,i+1] = 1.

print M[9,9], M[2,2], M[2,3]
```

Square brackets are used in indexing operations. If the square brackets contain only a single item, that item is passed to `getitem` and `setitem` as `key`. If the brackets contain a sequence of elements separated by commas, they are passed as a list, whence `key` has to be treated as a list, as in the example above. This example uses integers for indexing, but the indexing model in Python is completely general. Any Python objects may be used for indexing, including floats, complex numbers, strings, and even objects you have defined yourself.

One of the most powerful features of object-oriented programming is that you can define, or overload all the arithmetic operators so that they have the behavior you want when applied to your own objects. This allows you to design customized data types that allow you to condense very complicated operations into compact and simple statements. As a very simple example, let’s create a Gaussian integer data type, which behaves like a complex number, but uses long integers so as to allow unlimited precision. Python does not provide this as a native data type, but the following example allows us to do it ourselves:

```python
class gaussInt:
    def __init__(self, real, imag):
        self.real = real
        self.imag = imag
    def __add__(self, other):
        if (type(other) == type(1)) or (type(other) == type(1L)):
            return gaussInt(other+self.real, other+self.imag)
        else:
            return gaussInt(other.real+self.real, other.imag+self.imag)
    def __mul__(self, other):
        if (type(other) == type(1)) or (type(other) == type(1L)):
            return gaussInt(other*self.real, other*self.imag)
        else:
            return gaussInt(other.real*self.real-other.imag*self.imag,
                            other.imag*self.real + other.real*self.imag)
    def __repr__(self):
        return "%%d + %%d i"%(self.real, self.imag)
```

Note that the arithmetic methods create a new `gaussInt` object to return. Note also the type-checking, which allows arithmetic to be performed between Gaussian integers and regular integers. The class would be used as follows:

```python
x = gaussInt(3,5)
```
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```python
y = gaussInt(7,1)
x*3 + y*y
z = 1
for i in range(50):
    z = x*z
print z
```

The `__repr__` method in this example makes the object print out nicely when you type its name or use it in a `print` statement. Try leaving it out, and see what happens when you type the object’s name, or perform an arithmetic operation.

We have defined addition and multiplication for our Gaussian integers, but attempts to use subtraction, negation, mod, exponentiation or division will cause an error message, because these operations have not been defined. Each of these operations, and many more, have their own reserved method names that can be defined. There is no need to stick to uses of the operator symbols that resemble their customary use. You’re free to redefine addition as multiplication and multiplication as addition, if you want. More usefully, if you need a special symbol to represent matrix multiplication, you can redefine the mod operation `%` to mean matrix multiplication, leaving `*` to mean pointwise multiplication. Or, if you mostly use matrix multiplication, you can define `*` to mean matrix multiplication and `%` to mean pointwise multiplication.

A *commutative operator* (say, `*`) is one for which \( x * y = y * x \). Many operations, most commonly matrix multiplication, are non-commutative; one needs to keep track of the order of operation. All the binary operators can be made non-commutative in Python. In the Gaussian integer example, we didn’t need to think much about which operand in \( x*y \) was "self" and which one was "other", because the operation being implemented is commutative. To implement a non-commutative operation, you only need to pay attention to which operand is "self" and which is "other". The rule in Python is that in a binary operation such as \( x*y \), the first operand (\( x \)) is "self" and the second (\( y \)) is "other". As a simple example, let’s implement `*` as string concatenation, which is a non-commutative operation. For strings, Python already implements concatenation as the meaning of the operator `+`, so the only point of this example is to fix in the mind the somewhat confusing matter of which operand is "self" and which is "other". We define the class `nonCommutative`:

```python
class nonCommutative:
    def __init__(self,x): #x should be a string
        self.val = x
    def __mul__(self,other):
        return nonCommutative(self.val + other.val) #Concatenate strings
    def __repr__(self):
        return self.val
```

Now, if we create some instances:

```python
x = nonCommutative('a')
y = nonCommutative('b')
```

then \( x*y \) will evaluate to `ab` and \( y*x \) will evaluate to `ba`. Thus, to implement a noncommutative operation, you only need to keep in mind that "self" is the operand on the left and "other" is the operand on the right, in binary operations like `__add__` or `__mul__`. 
Since matrix multiplication is non-commutative, you would need to pay attention to this if you wanted to overload multiplication of \texttt{numpy} arrays so that \texttt{*} meant matrix multiplication instead of point-by-point multiplication. You don’t need to pay much attention, though, since the basic lesson is that if you keep the operands in the "natural" order, everything will work out fine. The following defines a new class of matrices, for which \texttt{*} is matrix multiplication and \texttt{\%} is pointwise multiplication:

\begin{verbatim}
class BetterArray:
    def __init__(self,array):
        self.array = array
    def __mul__(self,other):
        return BetterArray(numpy.matrixmultiply(self.array,other.array))
    def __mod__(self,other):
        return BetterArray(self.array*other.array)
\end{verbatim}

The array handed to \texttt{\_\_init\_\_} should be a \texttt{numpy} array, though this class doesn’t check to make sure that is the case. To try this out, let’s multiply the matrices

\[
X = \begin{bmatrix} 0 & 1 \\ 1 & 0 \end{bmatrix}, \quad Y = \begin{bmatrix} 0 & 1 \\ -1 & 0 \end{bmatrix}
\]

(2.1)

To create and multiply these arrays, and print out the result, type the following:

\begin{verbatim}
import numpy
X = BetterArray(numpy.array([[0,1],[1,0]]))
Y = BetterArray(numpy.array([[0,1],[-1,0]]))
Z = X*Y
print Z.array
Z1 = Y*X
print Z1.array
\end{verbatim}

Multiply out the arrays by hand to make sure our implementation of \texttt{BetterArray} handles the non-commutativity properly. Note that to get the results in the above example, we needed to do things like \texttt{\_\_repr\_\_} method for \texttt{BetterArray}. Without this, simply typing \texttt{X*Y} performs the operation, but tells us nothing useful about the result. \texttt{Z.array} is a \texttt{numpy} array, which knows how to print itself. \footnote{Unfortunately, the \texttt{\_\_repr\_\_} method of \texttt{numpy} arrays is buried in the compiled level of the implementation, and can’t easily be gotten at.}

As an exercise, complete the definition of the \texttt{BetterArray} class by defining addition, subtraction and negation, and try out the object. You can further extend the class by adding some type-checking of \texttt{other} so that the operations can handle the case of multiplication by a scalar. If you are really ambitious, you could even define matrix division, by incorporating a matrix inversion method for square matrices.

Python also provides methods for "right" versions of the binary operations, e.g. \texttt{\_\_rmul\_\_} and \texttt{\_\_radd\_\_}. If \texttt{y} has an \texttt{\_\_rmul\_\_} method and \texttt{x} has no \texttt{\_\_mul\_\_} method, then \texttt{x*\textup{y}} translates into a call to the \texttt{\_\_rmul\_\_} of the object \texttt{y} in which \texttt{y} is "self" and \texttt{x} is "other", i.e. \texttt{y.\_\_rmul\_\_(x)}.

It works similarly for other binary operations. As we’ve already seen, you do not need to use the "right" versions to make operations non-commutative. So what are the "right" versions good for? Our \texttt{gaussint} class provides an example of a case where you would need \texttt{\_\_rmul\_\_} and \texttt{\_\_radd\_\_.} If \texttt{z} is...
a `gaussInt` then `z*3` returns the correct answer because `z` has a `_mul_` method and this method checks if `other` is an integer and proceeds accordingly. However, `3*z` raises an error, because the integer has no way of knowing how to multiply itself by a `gaussInt`. The way out of this problem is to give the `gaussInt` class an `__rmul__` method:

```python
class gaussInt:
    ...
    def __rmul__(self,other):
        if (type(other) == type(1)) or (type(other) == type(1L)):
            return gaussInt(other*self.real,other*self.imag)
        else:
            return gaussInt(other.real*self.real-other.imag*self.imag,
                            other.imag*self.real + other.real*self.imag)
```

Now, `3*z` works, because `z` has an `__rmul__` method that Python can use. Note that, because we want `i*z` to give the same result as `z*i`, where `i` is an integer, we didn’t really need to copy the whole definition of `__mul__` into `__rmul__`, as we did above. As a shortcut, we could have written simply

```python
class gaussInt:
    ...
    def __rmul__(self,other):
        return self.__mul__(other)
```

Note that we invoke the `__mul__` method as `self.__mul__(other)` not as `self.__mul__(self,other)`. That is because the special `self` argument is only used in Python when we are defining a method, and never when we are just invoking (calling) it. As an exercise, extend the arithmetic of `gaussInt` further by adding an `__radd__` method.

Basically, the "right" versions of the binary operations are never needed if you only want to define operations between objects of the same type. You only need them to deal with operations between objects of differing types. Now here comes the confusing part. Suppose `x` has an `__add__` method and `y` has an `__radd__` method. How is `x+y` interpreted? Is it `x.__add__(y)` or `y.__radd__(x)`? The answer is that Python will implement the operation as `x.__add__(y)`. There is an important exception to this rule. Namely, certain very well-constructed objects will go on to try `y.__radd__(x)` if `x.__add__(y)` creates an error (and similarly for other binary operations). This is how Python was able to make sense of `3*z`, in our `gaussInt` example, even though integers already have a `__mul__` method, which you’d think would raise an error, since they don’t know how to multiply an algebraic integer by themselves. This kind of error trapping doesn’t happen automatically. It has to be built into the object. Integers, long integers, floats, complex numbers, strings, lists and `numpy` arrays are all well constructed objects in this sense.

In the case of the class `BetterArray`, it is a considerable nuisance that it is necessary to provide definitions of all the operations you want the object to handle, even if you don’t need to change their behavior (as in the case of addition and subtraction). Object oriented languages like Python provide a powerful way to handle this issue, in the form of inheritance. Use of inheritance to build daughter classes from existing ones will not be treated here. Other advanced

\[\footnote{Unfortunately, you can’t actually use inheritance with `numpy` arrays in this way, since the classes used in these arrays are implemented in efficient, compiled code. These object definitions are not accessible to the Python interpreter, and so most their methods cannot be inherited by objects defined at the Python level.}\]
object concepts we are leaving out include introspection and polymorphism. The eager student who wishes to dig deeper into object oriented programming can find excellent treatments of these subjects in virtually any complete Python programming handbook.

2.5.2 Getting input interactively

2.5.3 Dictionaries

2.5.4 Writing text data to files

The data writing and reading capabilities provided by the Curve object will probably take care of all the input-output needed to get through this course. At some point, you may be faced with the need for writing or reading files of a more general form. This section and the next covers the basics of how that is done.

First you need to open the file. To do this, you type

```
myfile = open('test.out','w')
```

where `myfile` is the object by which you will refer to the file in your Python program. You can use any variable name you want for this. Similarly, you can replace `test.out` with whatever you want the file to be called. The second argument of `open` says that we want to create a new file, if necessary, and allow the program to write to it.

You can only write a string to a file, so first you have to convert your data to a string. You have already learned how to do this. The following example serves as a reminder, and also shows how you can skip to a new line at the end of the string.

```
a = 1.
b=2.
outstring = '%f %f
'%(a,b)
```

The definition of `outstring` tells Python to make a string converting the elements of the tuple from floats to characters, with a space in between and a carriage return (newline) at the end of the line.

Files are objects in Python, so to write the string to the file, you just do `myfile.write(outstring)`.

Now you have everything you need to write space-delimited data to a file, except that when you are done, you need to close the file by executing `myfile.close()`.

Using what you have learned write a table of the functions \( x/(1 + x) \) and \( x^2/(1 + x^2) \) vs. \( x \) to a file. You can take a look at the resulting file in any text editor, or load the file into the program of your choice for plotting.

2.5.5 Reading text data from a file

To read text data from a file, you need to read in a line of text, and then convert the items into numbers, if that is what they represent. In order to do the conversion, it is necessary to know what
kinds of items are in the file, although strings have various methods that can help you identify whether an item is a number or not. Conversion is done by string-to-number routines found in the module `string`. Strings representing integers can be converted to float numbers, but if you try to convert a string representing a float to an integer, you will get an error.

The following example reads a single line from a file, which may consist of integers or floats separated by white-space characters, and converts it into a list of values. To read the rest of the file, you would repeat the procedure until the end of the file is reached.

```python
import string
f = open("myfile.txt")
buff = f.readline()
items = buff.split() # Or, do it all at once with items = f.readline().split()
values = [string.atof(item) for item in items]
```
Chapter 3

Appendix A: Hints for the user of Unix and its relatives

When I refer to “Unix,” in this workbook, it should be understood as applying to any unix-like operating system, including Linux, Mac OS X, Solaris or IRIX.

3.1 Simple Unix for the masses

It will be helpful to know a few basic Unix commands for manipulating files and directories. You can experiment with the following:

- `ls` lists the contents of the current directory (folder)
- `cd ...` changes to a new directory, e.g. `cd python` to change to the directory named `python`.
- `pwd` gives the name of the current directory
- `rm <name>` removes a file, e.g. `rm junkfile.py`
- `mv <oldname> <newname>` renames, or ”moves” a file, e.g. `mv test.py junk.py`
- `cp <sourcefilename> <destination>` copies `sourcefilename` to a new place. If `destination` is a file name (perhaps including a directory path) then `cp` makes copy of the source file with the new name, in the indicated place. If `destination` is a directory name, then a copy of the original file is placed in the indicated directory, keeping the same name as the original.
- `mkdir <name>` makes a new directory, e.g. `mkdir python`
- `rmdir <name>` removes a directory (which must be empty)
- `more <name>` lists the contents of a file, one page at a time

For writing programs and for various other chores, it will often be necessary to create and modify text files. For the purposes of this course, the text editor built into the Python Integrated Development Environment (discussed below) should be all anybody needs. Some stand-alone Unix text editors that may be of interest include `vi` (universally available but cryptic), `pico` (very simple to use, but somewhat limited in features) and `emacs` (very powerful and geek-friendly).
3.2 A few useful Unix utilities

3.3 Nasty Unix stuff I hope you won’t have to deal with

Now we need to discuss a few very technical Unix things related to the assuring that climate knows how to find various software and files that it needs. If your account on climate was set up properly by your sysadmin, you should need not need to take any action based on the following checks of the setup. However, if any of the checks fail, the information will help your sysadmin to set matters right, or alternatively will help your Unix-literate instructor guide you through the process of modifying your setup.

The first thing is to make sure that the commands you need are properly installed and can be found. Type `which python` and see what happens. If the response tells you the location of the command being used, then everything is OK. If the response complains that the command wasn’t found, then either python wasn’t installed or your account has not been set up to know how to find it. It’s most likely that your `PATH` variable, which tells the computer where to search for commands, hasn’t been set properly. You should ask your sysadmin to fix the problem, or to show you how to set up your `PATH` to find the commands you need. If you are using Matlab for data analysis and graphics, try `which matlab` to verify it’s availability. Similarly, if you are using ncl for graphics and data analysis, try `which ncl`. By the way, you can find out where the computer is looking for commands by typing `echo $PATH`.

The next thing is to check that Python knows where to find the scripts and extension modules you have written yourself, and the ones provided for general use by the class. Python always looks for scripts in your current directory (the one returned by the `pwd` command at the Unix prompt). It is handy, though, to set things up so that Python can find certain commonly used modules whichever directory you happen to be in. This is done via the `PYTHONPATH` variable. To check whether it’s been set properly, type `echo $PYTHONPATH`. You should get the result

```
<myhomedir>/modules:/home/ClimateCourse/modules
```

where `<myhomedir>` is the home directory for your account, i.e. the one you get back from a `pwd` right after you first log in. This setting means that Python will always look for any of your Python programs in the directory `modules` in your home directory, as well as in the course directory where your instructor has put Python modules that are meant to be generally available. If you find that `PYTHONPATH` hasn’t been set, or has been set incorrectly, you can either plead with your sysadmin to set things right, or you can take matters into your own hands. The problem is, that the right action to take depends on which ”shell” your account is set up to use. If you have no idea what your shell is, and have no inclination to find out, it is best to let your sysadmin handle things. The following instructions assume you are using `csh` or `tcsh`. Users of `sh` and `bash` need to do things slightly differently.

You can set `PYTHONPATH` manually every time you log in by typing the instructions `unsetenv PYTHONPATH` to get rid of any bad declaration there may be, followed by

```
setenv PYTHONPATH <myhomedir>/modules:/home/ClimateCourse/modules
```

where you need to replace `<myhomedir>` with the actual name of your home directory (on most systems, a tilde works as a shortcut for your home directory). Rather than executing this procedure each time you log on, it’s better to add it to a special file (`.login` for `csh`, `tcsh`) that is executed each time you log in. You just use a text editor (see below if you don’t yet know any) to create or edit the `.login` file and add the necessary lines. If you do this, you can skip the `unsetenv` step.
If you are using NCL for graphics then you have a few other things to check. Type `echo $NCARG_ROOT`. This tells you where the files needed by NCL have been installed. If it reports back as undefined, then you need to find out from the sysadmin where ncl is installed and set the value of NCARG_ROOT either manually or in your .login file. If you are having trouble using NCL it usually means that this variable has not been set properly. In addition, if you find that ncl crashes when you try to do a shaded contour plot or map, then you need to issue the command `limit stacksize unlimited` at the beginning of each session, or put it in your .login file. This is known to be necessary under Mac OSX.

If you are using Matlab there is an environment variable called MATLABPATH that needs to be set properly. Do an `echo $MATLABPATH` to find out what its value is. If your instructor wishes Matlab to automatically look for Matlab routines in the course directory `/home/ClimateCourse/matlab`, then this directory should be included in MATLABPATH. You can add it yourself if it isn’t there, as for PYTHONPATH. Depending on the particulars of your installation, there may need to be a few other directories in the path, associated with the routines needed for reading netCDF files. There’s little general advice that can be given with respect to this issue. If you are having trouble reading netCDF files in Matlab when you start doing the datalabs, then it is likely that either the MexCDF add-on package has not been installed or has been improperly installed. This is something that your sysadmin will have to deal with.
Appendix B: Setting up the software

This section is intended to help the instructor or course assistant in setting up the software environment for the course.

3.4 Public domain software to install on the server

Either on a server, or on each individual student workstation, the following public domain software needs to be installed:

- An implementation of Python 2.3 or better, including the \texttt{Numeric} array package and the \texttt{idle} integrated development environment. On Unix-like systems (including Mac OS X), graphics is done via the X windowing system. This is needed for \texttt{idle} as well as other graphical display tasks. You should make sure that you have (or install) a full Python installation, which includes X or equivalent graphics support.

Most Linux installations include a full-featured Python suite by default. You can check this out by entering the Python interpreter (type \texttt{python}, or perhaps \texttt{python2.3}) then do \texttt{import Numeric}. to see if the array package is there. To make sure you have X windows support, and the integrated development editor, type \texttt{idle}.

Mac OS X comes with a pre-installed Python, but it is a bare-bones installation lacking most of the add-ons that make Python useful, in particular \texttt{idle} and \texttt{Numeric}. It’s best to do a fresh installation, using the \texttt{fink} system. Go to \texttt{fink.sourceforge.net} and follow the instructions there.

Note that the X11 server is not installed by default on Macs. If it’s not there, you will need to install it on the student workstations and the server machine, from the OSX install disk. Also, the server machine will need the Developer Tools suite (called ”Xcode” in OS 10.3) and the x11 SDK toolkit, both installed from the Xcode developer tools disk. These files are needed in order for the \texttt{fink} system to build and install new software.

Excellent full-featured Python implementations are available for Microsoft Windows, and most of the exercises in the workbook can be done on such a system. However, the plotting software provided with the courseware will not work with Windows, and the \texttt{cdms} package used for \texttt{netCDF} file manipulation in the later data analysis chapters is not available for Windows. The rest of the courseware will work fine. Students can use a Windows implementation on their own machines to do most of the computational exercises, and can dump
text output to a file for plotting in the graphical program of their choice. There is no good
public-domain solution for working with netCDF files on Windows. If you want students to do
the geographically mapped data analysis exercises in the later chapters, it will be necessary
to provide access to a Linux or Mac OS X server. These data analysis exercises, can also be
easily adapted to Matlab, which can also read and manipulate netCDF files with suitable add-
on libraries. That comes at the expense, however, of losing the more powerful programming
features of Python.

• To do graphics, you need the Ngl module. It can be downloaded from [**Ngl_URL]. A Mac
version is provided on the courseware site, in the pre-built distribution. If you intend to
do your graphics outside Python, you do not need any of this. Ngl requires X windows for
its graphics. It will work on Mac OS X and virtually any Linux or Unix system, but is not
available for the Microsoft Windows operating system. If you have a lab that has Microsoft
Windows machines as workstations, the best thing to do is to install the course software on a
Linux or Mac OS X server, and have the students log into it from the Windows workstations
using a public domain X server such as CygWin.

• Analysis of data stored in plain text files, such as the paleoclimate time series in Chapter 1
and the soundings in Chapter 2, can be done without any special software other than the
modules provided as part of the courseware. These modules are plain Python scripts, and
will work on any Python installation that has numpy. A few of the results shown in the later
chapters are derived from binary data that was originally in netCDF format. None of the
exercises actually require the student to be able to work with such data files, but the if one
wants to reproduce the corresponding figures given in the book, one will need to be able
to read netCDF. The easiest way to do this if you are already installing PyNgl is to install
PyNio at the same time, since it comes from the same place and installs in pretty much the
same way. Another excellent Python interface to netcdf is the CDAT module. This installs
very easily on Linux, somewhat less so on Mac OS X.

• It is also recommended that you install the Unix utility ps2pdf, which converts a Postscript
file to Acrobat pdf form. The Ngl graphics module can produce Postscript output, and
ps2pdf provides an easy way for the students to convert this into a file that can be posted
on a web site, incorporated in a lab report, emailed to the instructor, or just printed out. If
the instructor provides a simple html template for the student to use, lab reports can even
be turned in in the form of a simple web page, which the student can put in his or her www
or public_html directory.